

From: Thomas Hockey et al. (eds.). *The Biographical Encyclopedia of Astronomers*, Springer Reference. New York: Springer, 2007, pp. 631-633

Courtesy of  Springer  
science+business media

[http://dx.doi.org/10.1007/978-0-387-30400-7\\_763](http://dx.doi.org/10.1007/978-0-387-30400-7_763)

## Khwārizmī: Muḥammad ibn Mūsā al-Khwārizmī

Sonja Brentjes

---

**Born circa 780**

**Died circa 850**

Khwārizmī was a well-known astronomer and mathematician who spent most, if not all, of his scholarly life in Baghdad, in close connection with the 'Abbāsīd court, particularly during the caliphate of **Ma'mūn** (reigned: 813–833). There is some confusion about his origins. The 10th-century bibliographer Ibn al-Nadīm claimed that Muḥammad ibn Mūsā was from Khwārizm in Central Asia, whereas the historian Ṭabarī reported that Khwārizmī was also known as al-Quṭrabbulī, a name associating the scholar with a town not far from Baghdad rather than with the Central Asian region of Khwārizm (Toomer, p. 358). Ṭabarī added that he was also called al-Majūsī, a designation that indicates that Khwārizmī was a Zoroastrian rather than a Muslim. Ibn al-Nadīm also stated that he was attached to the *Bayt al-ḥikma*, the caliphal library. What this means exactly is unclear since there is considerable modern controversy about this institution and whether it should be regarded simply as a library or as a translation bureau and scientific research institution.

Ibn al-Nadīm lists four astronomical works: the *Zīj al-Sindhīd* (an astronomical handbook according to the *Sindhīd*), a treatise on the sundial, and two works on the astrolabe. Of these, the first is no longer extant in Arabic but is available in Latin translation; the second seems to be extant as are fragments of a work on the astrolabe. Rosenfeld and Ihsanoğlu list 20 astronomical works in all. Among Khwārizmī's nonastronomical works at least two are mathematical: a book on Indian arithmetic and one devoted to algebra. (A book on "addition and subtraction" is also attributed to him.) He also has a *Book on Geography*, which is extant, and a *Book on History*, which is not but was quoted by later authors. The *Algebra* and the *Zīj* were dedicated to Caliph Ma'mūn. The treatise on Indian arithmetic in its extant Latin translation mentions the *Algebra* and hence was produced later. Khwārizmī also wrote a description of the Jewish calendar, which was written not before 823/824 because one of its examples is carried out for that year. The other texts offer no clue for dating them.

Khwārizmī's *Zīj al-Sindhīd* confirmed the place of pre-Islamic Indian astronomical models, functions, and parameters in the scholarly community of Baghdad, which had been multicultural since the second half of the 8th century. Before him, several "Zījāt al-Sindhīd" are said to have been compiled based on Arabic translations of Indian astronomical handbooks (Pingree 1970, p. 105). Indeed, the astronomer **Ibn al-Ādamī** described Khwārizmī's *Zīj* as an abridgment, prepared for Ma'mūn, of **Fazārī**'s (second half of the 8th century) handbook *al-Sindhīd* (Pingree 1970, p. 106). Khwārizmī's tables were known to astronomers not only in Baghdad, but also in Central Asia in the east and in Andalusia on the Iberian Peninsula in the west. A number of authors who compiled their own handbooks relied on it. Two examples are the already-mentioned Ibn al-Ādamī in Baghdad, in his nonextant astronomical handbook *Naẓm al-'iqd*, and **Ibn Mu'ādh** in Andalusia, whose handbook is extant in its Latin translation *Tabulae Jahan*. Others commented on Khwārizmī's tables, often criticizing the methods used, such as **Aḥmad ibn Kathīr al-Farghānī** (9th century) in Baghdad, Ibn al-Muthannā (10th century?) in Andalusia, 'Abdallāh ibn Masrūr al-Ḥāsib al-Naṣrānī in Baghdad (9/10th centuries), and **Abū Rayḥān al-Bīrūnī** in Ghazna. Bīrūnī devoted three treatises to Khwārizmī's *Zīj*. In one of them he defended Khwārizmī against attacks of Aḥmad ibn al-Ḥusayn al-Ahwāzī (10th century) (Muḥammad ibn Mūsā 1983, p. 21). It is believed that as late as the 19th century, tables connected to Khwārizmī's *Zīj* were copied in Egypt (Goldstein and Pingree 1978; Pingree 1983).

No copy of Khwārizmī's *Zīj* has survived, but Hebrew and Latin versions of various later texts connected with Khwārizmī's tables are extant. Ibn al-Muthannā in Andalusia set out to compose a commentary in order to rectify the obscurities of a critique of Khwārizmī's tables written by Farghānī. Both commentaries are lost. But Hebrew and Latin versions of Ibn al-Muthannā's commentary are extant (Goldstein 1967, pp. 5-6; Pedersen, p. 32). The Latin translation of Ibn al-Muthanna's commentary was made by Hugo of Santalla (12th century) (Millás Vendrell, 1963). One Hebrew translation was produced by [Abraham ibn Ezra](#) (Goldstein 1967, p. 3). In the same century as Ibn al-Muthannā and also in Andalusia, [Maslama ibn Aḥmad al-Majrīṭī](#) edited Khwārizmī's tables. Majrīṭī's student [Ibn al-Saffār](#) is believed to have continued the editorial work of his teacher (Toomer, p. 358). This edition was translated in the 12th century into Latin presumably by [Adelard of Bath](#). Other Latin manuscripts contain texts that seem to combine extracts from Ibn al-Muthannā's commentary, Majrīṭī's edition, and one or more Arabic compilations of material, translated and revised into Latin, from the tables of Khwārizmī, [Yahyā ibn Abī Mansūr](#), [Muḥammad ibn Jābir al-Battānī](#), Ibn al-Muthannā, and Majrīṭī (Pedersen, pp. 31-46). The *Toledan Tables*, compiled around 1060 in Muslim Spain, contain several tables from Khwārizmī's *Zīj*, some of which are not found in Majrīṭī's revision. They are lost in Arabic, but extant in several Latin versions (Dalen, p. 200).

The extant texts and tables follow in their presentation of the material; in their methods, rules, and models; and in several of their parameter values astronomical knowledge and practice as taught in several treatises written by Hindu scholars between the 5th and 7th centuries. They also use elements from Sasanian astronomical tables, incorporate borrowings from Greek astronomical writings (in particular [Ptolemy's](#) *Almagest* and *Handy Tables*), and include values determined by observations carried out during Ma'mūn's reign. A survey of the character of the tables in the Latin translation of Majrīṭī's revision of Khwārizmī's *Zīj* has recently been given by Dalen (pp. 200-211). Khwārizmī's original *Zīj* has been described as a similar mixture of elements by Ibn al-Ādamī, who, according to Ibn al-Qiftī (1173-1248), had reported that Khwārizmī had relied in his work on the mean motions of the Indian tradition, but differed from it in the equations and the declination. Ibn al-Ādamī also asserted that Khwārizmī followed Sasanian sources with regard to the equations and Ptolemy when he dealt with the declination of the Sun (Pingree 1970, p. 106). According to McCarthy and Byrne, Khwārizmī's original handbook juxtaposed tables, which addressed the same kind of tasks, but came from different cultural origins. Examples illustrating the diverse components in the extant texts and tables and their modifications are the replacement of the Yazdagird calendar by the Hijra era, the addition of calendars alien to the traditions in India such as the ancient Egyptian, Seleucid, Roman, and Christian eras, the use of theorems (such as the Menelaus theorem) that were unknown to Hindu astronomers, the use of the value for the obliquity of the ecliptic as found in Ptolemy's *Handy Tables*, the use of the Ptolemaic value of  $66 \frac{2}{3}$  miles for a terrestrial degree, and the replacement of the latitude of Baghdad by the latitude of Cordova (Neugebauer, p. 19; Kennedy and Janjanian, pp. 73, 77; Goldstein 1967, pp. 7-8; Dalen, 1996, pp. 196, 240).

Khwārizmī's treatise on the Jewish calendar gives rules for determining the mean longitude of the Sun and the Moon based on this calendar and for determining on what day of the Muslim week the first day of the New Year shall fall. It also discusses the 19-year intercalation cycle and the temporal distance between the beginning of the Jewish era, *i. e.*, the creation of Adam and the beginning of the Seleucid era (Kennedy, 1964, pp. 55-59; Toomer, p. 360). The treatise on how to work with an astrolabe is only fragmentarily preserved, and opinions vary as to whether these fragments in their present-form represent the genuine version of what Khwārizmī actually wrote. The treatise on how to construct an astrolabe seems to be lost. Khwārizmī's book on geography *Kitāb Šūrat al-ard* combines substantial parts of Ptolemy's *Geography* with many non-Ptolemaic coordinates and place names. His two writings on arithmetic, one in the tradition of oral reckoning and the other according to the Indian tradition of written reckoning using the decimal place-value system, are lost in Arabic. The latter is extant in various Latin manuscripts. Khwārizmī's book on algebra is the first known in Arabic. It treats quadratic equations, the measurement of areas and volumes, commercial problems by means of four proportional quantities, and several types of Muslim inheritance mathematics. This text too was translated into Latin by at least two translators. Its influence upon elementary algebra in Arabic, Persian, Ottoman Turkish, Latin, and European vernacular languages was substantial.

Finally, it is worth mentioning that Khwarizmi may have participated in a number of scientific expeditions, one to measure the size of the Earth, the other to explore the regions north of the Caspian Sea (Matvievskaya and Rozenfeld, 1983, Vol. 2: p.41). The first, though, has been recently questioned (King, 2000).

---

## Selected References

- Al-Khwārizmī, Muḥammad ibn Mūsā (1983). *Astronomicheskiye traktaty*. Vstupitel'naja stat'ja, perevod i komentarii A. Ahmedova. Tashkent: Izdatel'stvo "FAN" Uzbekskoj SSR.
- (1997). Texts and Studies II. Collected and reprinted by Fuat Sezgin, in collaboration with Mazen Amawi, Carl Ehrig-Eggert, and Eckhard Neubauer. *Islamic Mathematics and Astronomy*, Vol. 4. Frankfurt am Main: Institute for the History of Arabic-Islamic Science at the Johann Wolfgang Goethe University.
- Dalen, Benno van (1996). "Al-Khwārizmī's Astronomical Tables Revisited: Analysis of the Equation of Time." In *From Baghdad to Barcelona: Studies in the Islamic Exact Sciences in Honour of Prof. Juan Vernet*, edited by Josep Casulleras and Julio Samsó. Vol. 1, pp. 195-252. Barcelona: Instituto "Millás Vallicrosa" de Historia de la Ciencia Árabe.
- Goldstein, Bernard R. (1967). *Ibn al-Muthannā's Commentary on the Astronomical Tables of al-Khwārizmī*. Two Hebrew versions, edited and translated, with an astronomical commentary by Bernard R. Goldstein. New Haven: Yale University Press.
- Goldstein, Bernard R. and David Pingree. (1978). "The Astronomical Tables of al-Khwārizmī in a Nineteenth Century Egyptian Text." *Journal of the American Oriental Society* 98: 96-99.
- Gutas, Dimitri (1998). *Greek Thought, Arabic Culture: The Graeco-Arabic Translation Movement in Baghdad and Early 'Abbāsīd Society (2nd-4th/8th-10th centuries)*. London: Routledge.
- Hogendijk, Jan P. (1991). "Al-Khwārizmī's Table of the 'Sine of Hours' and the Underlying Sine Table." *Historia scientiarum* 42: 1-12.
- Ibn al-Nadīm (1970). *The Fihrist of al-Nadīm: A Tenth-Century Survey of Muslim Culture*, edited and translated by Bayard Dodge. 2 Vols. New York: Columbia University Press.
- Kennedy, E. S. (1964). "Al-Khwārizmī on the Jewish Calendar." *Scripta mathematica* 27: 55-59. (Reprinted in Kennedy, *Studies*, pp. 661-665.)
- Kennedy, E. S., et al. (1983). *Studies in the Islamic Exact Sciences*, edited by David A. King and Mary Helen Kennedy. Beirut: American University of Beirut.
- Kennedy, E. S. and Mardiros Janjanian (1965). "The Crescent Visibility Table in Al-Khwārizmī's Zij." *Centaurus* 11: 73-78. (Reprinted in Kennedy, *Studies*, pp. 151-156).
- Kennedy, E. S. and Walid Ukashah (1969). "Al-Khwārizmī's Planetary Latitude Tables." *Centaurus* 14: 86-96. (Reprinted in Kennedy, *Studies*, pp. 125-135.)
- King, David A. (1983). "Al-Khwārizmī and New Trends in Mathematical Astronomy in the Ninth Century." *Occasional Papers on the Near East* 2. New York: New York University, Hagop Kevorkian Center for Near Eastern Studies.
- (1987). "Some Early Islamic Tables for Determining Lunar Crescent Visibility." In *From Deferent to Equant: A Volume of Studies in the History of Science in the Ancient and Medieval Near East in Honor of E. S. Kennedy*, edited by David A. King and George Saliba, pp. 185-225. *Annals of the New York Academy of Sciences*, Vol. 500. New York: New York Academy of Sciences. (Reprinted in King, *Astronomy in the Service of Islam*, II. Aldershot: Variorum, 1993.)
- (2000). "Too Many Cooks ... A New Account of the Earliest Muslim Geodetic Measurements." *Suhayl* 1: 207-241.
- Kunitzsch, Paul (1987). "Al-Khwārizmī as a Source for the *Sententie astrolabii*." In *From Deferent to Equant: A Volume of Studies in the History of Science in the Ancient and Medieval Near East in Honor of E. S. Kennedy*, edited by David A. King and George Saliba, pp. 227-236. *Annals of the New York Academy of Sciences*, Vol. 500. New York: New York Academy of Sciences. (Reprinted in Kunitzsch, *The Arabs and the Stars*, IX. Northampton: Variorum Reprints, 1989.)
- Matievskaya, G. P. and B. A. Rozenfeld (1983). *Matematiki i astronomi musulmanskogo srednevekovya i ikh trudi (VIII-XVII vv.)* (Mathematicians and astronomers of the Muslim middle ages and their works [VIII-XVII centuries]). 3 Vols. Moscow: Nauka.

McCarthy, Daniel P. and John G. Byrne (2003). "Al-Khwārizmī's Sine Tables and a Western Table with the Hindu Norm of  $R = 150$ ." *Archive for History of Exact Sciences* 57: 243-266.

Millás Vallicrosa, José María (1963). "La autenticidad del comentario a las Tablas astronómicas de al-Jwārizmī por Aḥmad ibn al-Muṭannā." *Isis* 54: 114-119.

Millás Vendrell, Eduardo (1963). *El comentario de Ibn al-Mutannā a las Tablas astronómicas de al-Jwārizmī*. Madrid.

Neugebauer, Otto (1962). *The Astronomical Tables of al-Khwārizmī*. Translation with commentaries of the Latin version edited by H. Suter, supplemented by Corpus Christi College MS 283. Copenhagen: Ejnar Munksgaard.

Pedersen, Fritz S. (1992). "Alkharizmi's Astronomical Rules: Yet Another Latin Version?" *Cahiers de l'Institut du moyen âge grec et latin* 62: 31-75.

Pingree, David (1968). "The Fragments of the Works of Ya'qūb ibn Ṭāriq." *Journal of Near Eastern Studies* 27: 97-125.

——— (1970). "The Fragments of the Works of al-Fazārī." *Journal of Near Eastern Studies* 29: 103-123.

——— (1983). "Al-Khwārizmī in Samaria." *Archives internationales d'histoire des sciences* 33: 15-21.

Rosenfeld, B. A. and Ekmeleddin Ihsanoğlu (2003). *Mathematicians, Astronomers, and Other Scholars of Islamic Civilization and Their Works (7th-19th c.)*. Istanbul: IRCICA, pp. 21-26.

Rosenfeld, Boris A. and N. D. Sergeeva (1977). "Ob astronomicheskikh traktatakh al-Khorezmi." *Istoriko-Astronomicheskie Issledovaniya* 13: 201-218.

Sezgin, Fuat. *Geschichte des arabischen Schrifttums*. Vol. 5, *Mathematik* (1974): 228-241; Vol. 6, *Astronomie* (1978): 140-143; Vol. 7, *Astrologie-Meteorologie und Verwandtes* (1979): 128-129. Leiden: E. J. Brill.

Suter, Heinrich (1914). *Die astronomischen Tafeln des Muḥammed ibn Mūsā al-Khwārizmī in der Bearbeitung des Maslama ibn Aḥmed al-Madrīṭī und der lateinischen Übersetzung des Adelhard von Bath*. Copenhagen: Kongelige Danske Videnskabernes Selskab. (Reprinted in Suter, *Beiträge zur Geschichte der Mathematik und Astronomie im Islam*. Vol. 1, pp. 473-751. Frankfurt am Main, 1986.)

Toomer, Gerald J. (1973). "Al-Khwārizmī." In *Dictionary of Scientific Biography*, edited by Charles Coulston Gillispie. Vol. 7, pp. 358-365. New York: Charles Scribner's Sons.